

The centripetal force  $F$  on mass  $m$  travelling in a circle with angular velocity  $\omega$  (radians / s) is given by

$$F = mr\omega^2$$

The force necessary to produce an acceleration  $a$  in a mass  $m$  is given by

$$F = ma$$

Thus we can derive the centripetal acceleration

$$mr\omega^2 = ma$$

$$a = r\omega^2$$

Now we require that  $a=g$ , and to solve for  $\omega$ ; thus we have

$$\omega^2 = \frac{g}{r}$$

$$\omega = \sqrt{\frac{g}{r}}$$

An angular velocity of  $\omega$  rad/s is equal to  $\omega/2\pi$  revolutions / second or  $60\omega/2\pi$  rpm. This is  $9.549 \omega$ , expressed to 3dp. The angular velocity  $\Omega$  rpm needed to produce an acceleration of  $g$ , is therefore given by

$$\Omega = 9.549 \sqrt{\frac{g}{r}}$$

$$= 9.549 \sqrt{g} \frac{1}{\sqrt{r}}$$

Taking  $g=9.807$ , we have  $\sqrt{g} = 3.132$ , and thus

$$\Omega = (9.549)(3.132) \frac{1}{\sqrt{r}}$$

$$= 29.907 \frac{1}{\sqrt{r}}$$

$$\approx 30 \frac{1}{\sqrt{r}}$$